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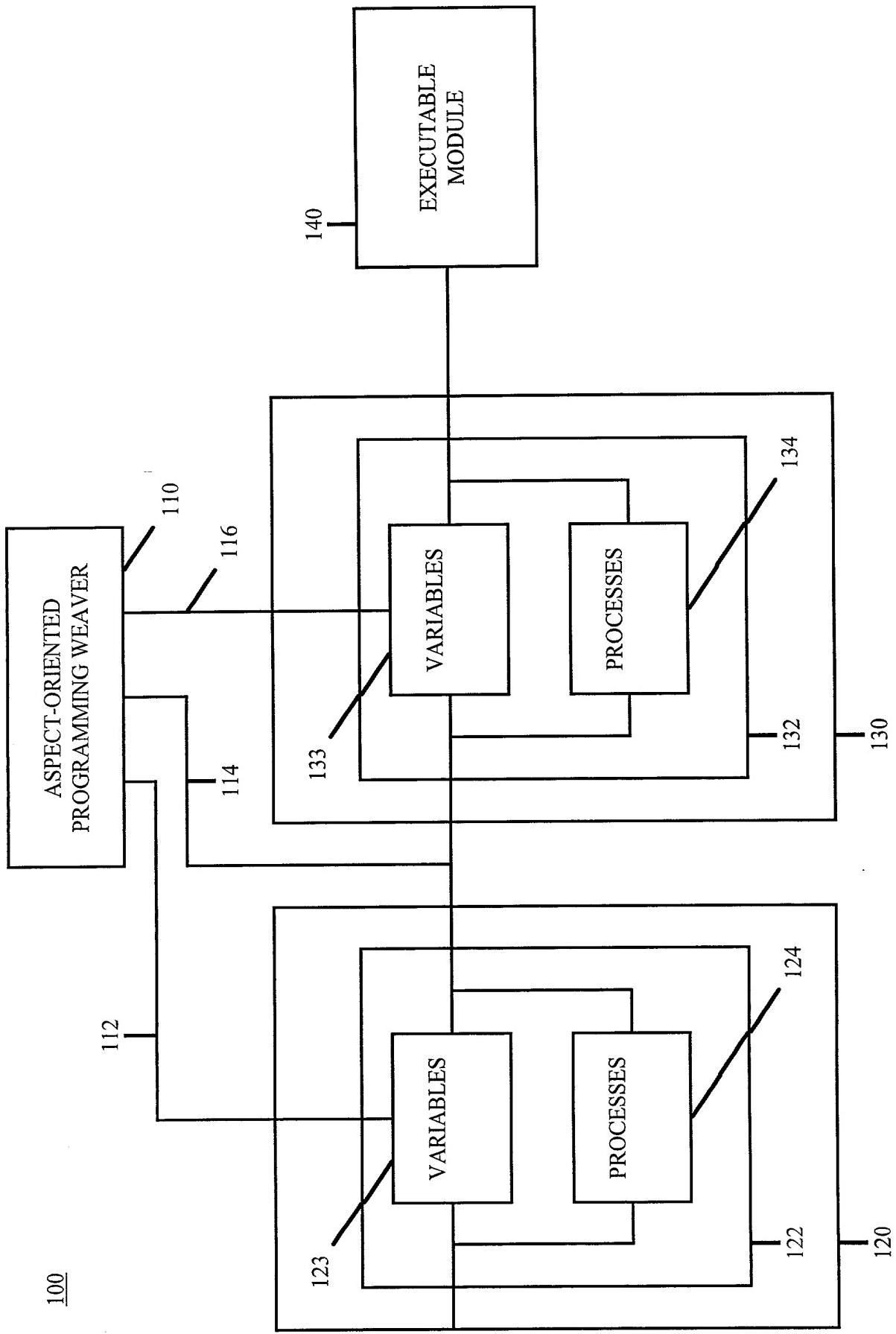


FIG. 1

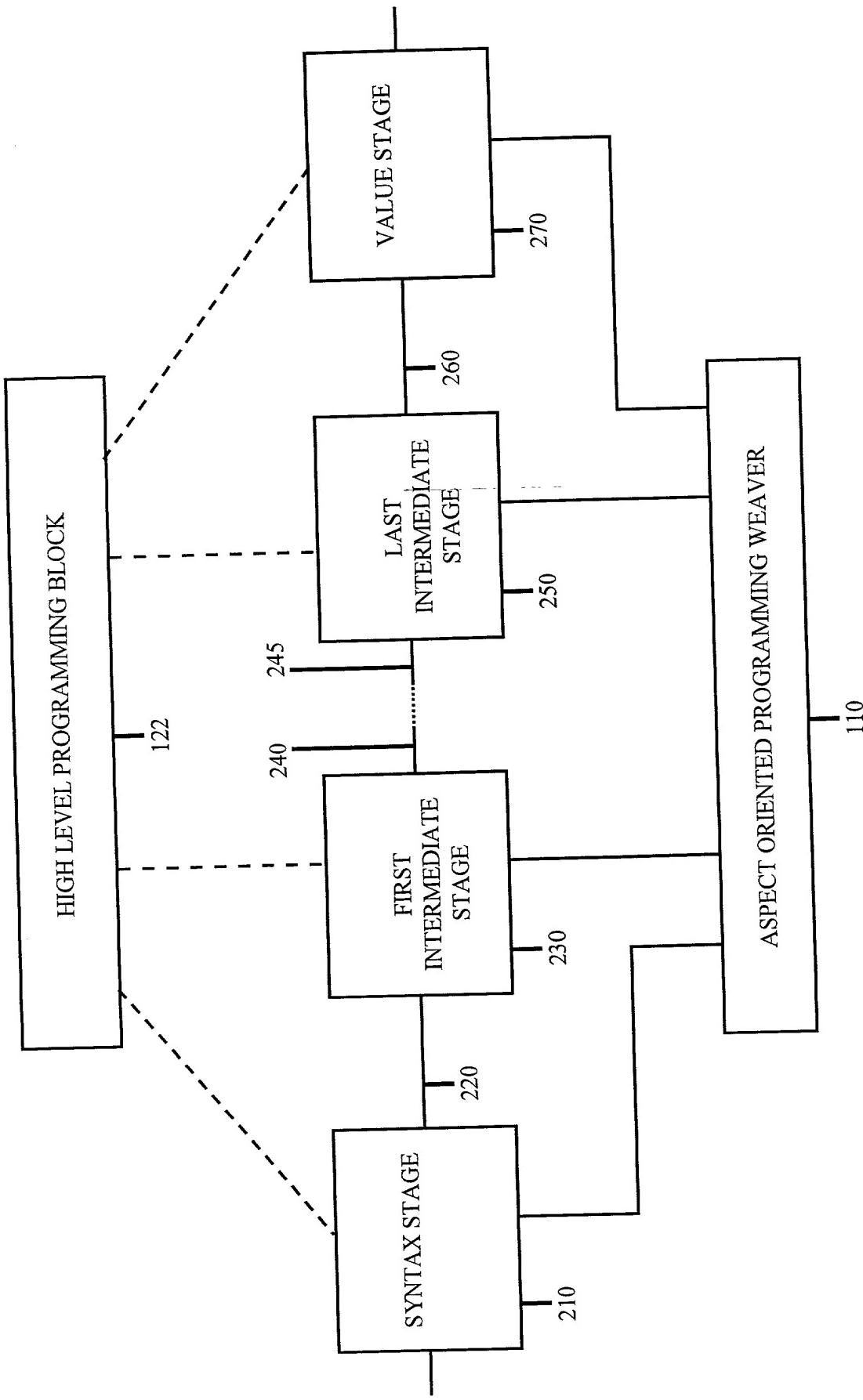


FIG. 2

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1 (stage requested-loops)
2 (projection key :defined-on requested-loops)
3 (projection computing-loop :defined-on requested-loops)
4 (define test
5   (lambda (x y z)
6     (and! (and! X y) z)))
7 (define and!
8   (reduction-stage requested-loops
9     (lambda (arg1 arg2)
10       (pointwise #'and arg1 arg2))))
11 (propagator requested-loops :bottom-up
12   (lambda (term)
13     (case requested-loops term
14       ((pointwise op arg1 arg2) (op arg1 arg2)
15        (let ((starting-loop
16              (fuse-loops (get-or-make-loop arg1) (get-or-make-loop arg2))
17              (my-key (gensym)))
18              (deconstruct requested-loops starting-loop
19                (ptw-loop fn inputs outputs) (fn inputs outputs)
20                (let* ((new-fn (reduction-stage computation
21                  (lambda (args)
22                    (let* ((temp (fn args))
23                      (result
24                        (op (find (key arg1) temp)
25                        (find (key arg2) temp))))
26                        (cons (cons my-key result)
27                          temp))))
28                      (new-loop (defer (ptw-loop new-fn inputs outputs))))
29                      (update (key value) my-key)
30                      (update (computing-loop value) new-loop))
31                      (if (computing-loop arg1)
32                        (update (computing-loop arg1)
33                          (defer (loop-reference value))))
34                      (if (computing-loop arg2)
35                        (update (computing-loop arg2)
36                          (defer (loop-reference value))))))))
37                      (else (note-demands value)
38                      )))))
39

```

FIG. 3A

```

39  (define get-or-make-loop (value)
40    (if (and (same-frequency value) (computing-loop value))
41        (get-loop value)
42        (defer (ptw-loop
43              (reduction-stage computation
44              (lambda (args) args)
45              (list (cons (key value) value))
46              nil))))
47  (define get-loop
48    (reduction-stage computation
49    (lambda (value)
50      (computing-loop (get-loop-location value)))))
51  (define get-loop-location
52    (reduction-stage computation
53    (lambda (value)
54      (case requested-loops (computing-loop value)
55      ((loop-reference next) (next)
56      (get-loop-location next))
57      (else value))))
58  (define note-demands (value)
59    (case requested-loops value
60      ((fn . args) (fn args)
61      (record-demand fn)
62      (map args #record-demand))
63      ((case stage value (pattern vars body) (else otherwise))
64      (stage value pattern vars body otherwise)
65      (record-demand value)
66      (record-demand body)
67      (record-demand otherwise))
68      ((lambda vars body) (vars body)
69      (record-demand body))))
70  (define record-demand (value)
71    (if (computing-loop value)
72        (let ((place (get-loop-location value)))
73          (key (key value)))
74        (case requested-loops (computing-loop place)
75        ((ptw fn inputs outputs) (fn inputs outputs)
76        (if (not (member key outputs))
77            (let ((new-outputs (cons key outputs)))
78            (update (computing-loop place)
79              (delay (ptw fn inputs new-outputs))))))))
80

```

FIG. 3B

```

80  (define ptw-loop
81    (lambda (fn inputs outputs)
82      (let ((output-pairs (early-mapcar (reduction-stage computation
83                      (lambda (key) (cons key (new-array)))
84                      outputs))))
85        (dotimes ((i 0 99))
86          (let* ((input-scalars
87                 (early-mapcar (reduction-stage computation
88                     (lambda (pair)
89                      (let ((key (first pair))
90                          (array (second pair)))
91                        (cons key (elt array i)
92                          inputs)))
93                      (output-scalars (fn input-scalars))))
94            (early-map (reduction-stage computation
95                (lambda (pair)
96                  (let ((key (first pair))
97                      (array (second pair)))
98                    (setf (elt array i)
99                      (find key output-scalars)))))))
99          output-pairs))))))
100
101 (define pointwise (fn op1 op2 => result)
102   (reduction-stage computation ;; inlineable after loop fusion
103     (find (key result) (get-loop result))))
104 (define fuse-loops
105   (lambda (loop1 loop2)
106     (if (stage-eq requested-loops loop1 loop2)
107         loop1
108         (deconstruct loop-structure loop1
109           ((ptw-loop fn1 inputss1 outputs1) (fn1 inputs1 outputs1)
110             (deconstruct loop-structure loop2
111               ((ptw-loop fn2 inputs2 outputs2) (fn2 inputs2 outputs2)
112                 (let ((inputs (merge inputs1 inputs2))
113                     (outputs (append outputs1 outputs2)))
114                   (ptw-loop
115                     (preserves computation
116                       (lambda (inputs) (merge (fn1 inputs) (fn2 inputs)))
117                         inputs outputs))))))))
118 (define find
119   (reduction-stage computation ;; inlineable after loop fusion
120     (lambda (id list)
121       (deconstruct computation list
122         (cons (cons key value) rest) (key value rest)
123         (if (stage-eq computation key id)
124             value
125             (find id rest)))))))
126 (define merge
127   ... like find

```

FIG. 3C

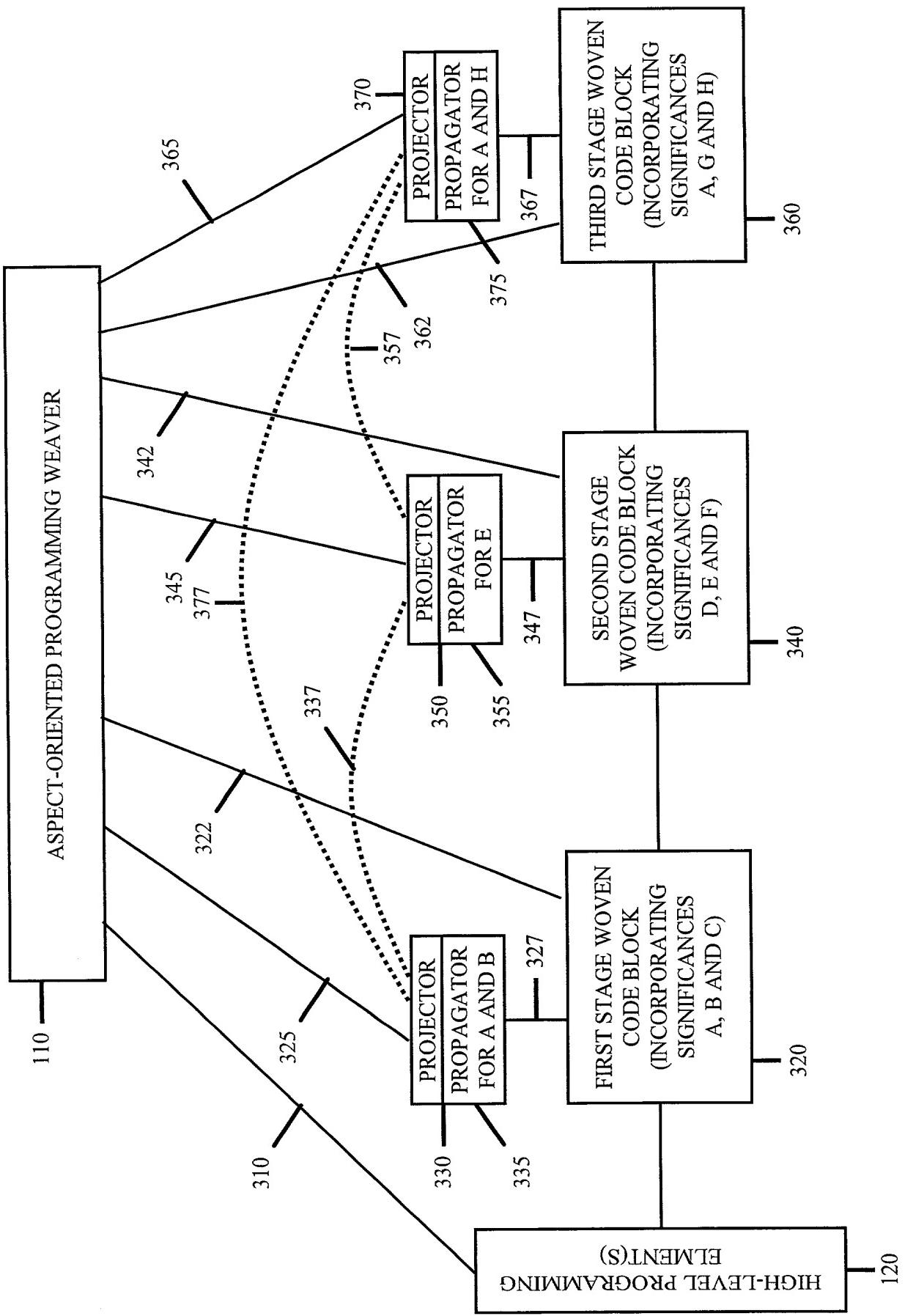


FIG. 4

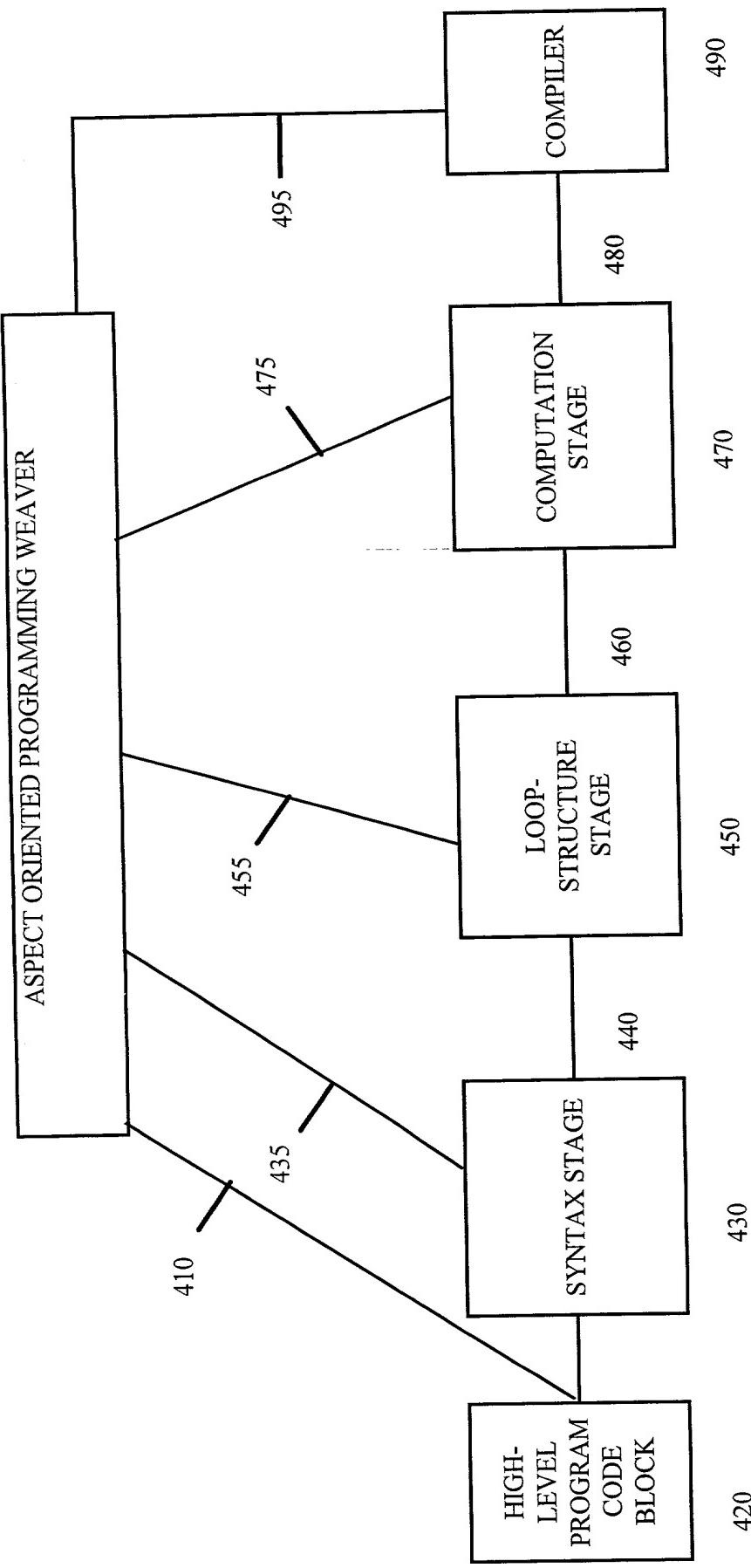


FIG. 5